

# A New Method for Estimating Causal Model Learning Accuracy

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You learned causal model  $M$  from real world data  $D$  generated from unknown true model  $T$ .

## Question:

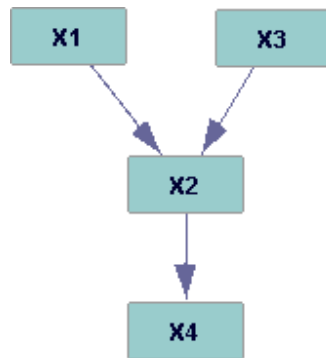
How close is  $M$  to  $T$ ?

# Solution Strategies

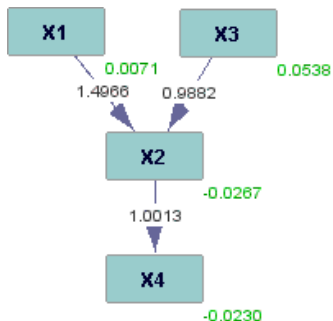
- **Statistical measures of fit:** individual score is not informative; best fit could still be inaccurate
- **Benchmark simulations:** incomplete; may not apply to this type of data; may not even be able to know if they apply
- **Resimulation:** benchmark against data that is similar to  $D$

# Resimulation 0: Data $D_1$ and Learned Graph $G_1$

X1	X2	X3	X4
0.3596	-1.2491	-2.9277	-3.5328
1.2639	4.0011	1.2282	4.1915
0.8749	-1.7419	-1.6859	-2.2926
-2.1222	-0.3536	2.465	-0.2342
-0.9151	-2.7165	-2.3928	-4.5982
-0.5706	-3.802	0.0331	-4.7854
1.2468	0.5542	-0.7107	1.0888
1.1232	5.1059	0.7407	6.571
-1.4056	1.5811	-0.527	0.5514
-0.2384	0.7289	-0.133	0.8222
0.0751	-2.5419	-1.708	-1.8866
0.8523	2.0218	0.6163	2.7466
0.2440	0.7100	0.6777	0.0002



# Resimulation 1: Fit $G_1$ to $D_1$ , making model $M_1$



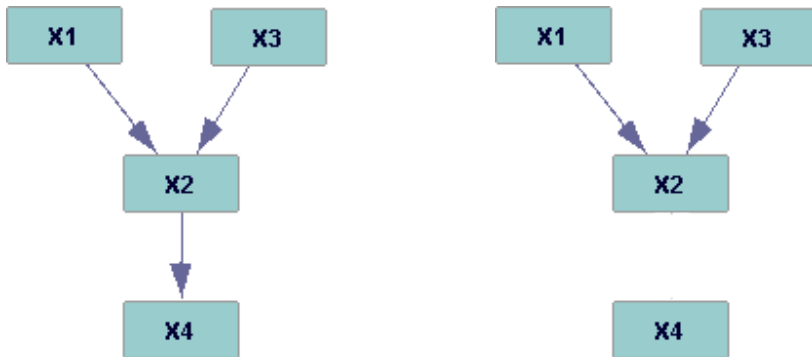


## Resimulation 2: Sample $D_2$ from $M_1$

X1	X2	X3	X4
0.8708	-4.2755	-3.8422	-1.4316
-0.4746	0.2453	2.3116	3.6107
-0.8326	1.6374	1.3244	-1.3061
0.8904	1.3817	0.5551	1.6176
-1.5868	-0.2379	-0.8964	-0.4021
0.9449	-0.4699	-1.6115	-0.4532
-1.4363	-1.9608	-0.0541	-2.2113
-0.1365	-1.5573	0.0807	0.2054
2.7841	6.6639	2.0372	7.3468
0.2111	-0.9978	-0.3473	1.5266
-0.6065	3.208	1.9332	4.4616
0.9039	-0.7902	-0.1446	-0.7825

Each row sampled from  $P_{M_1}(X_1, X_2, X_3, X_4)$

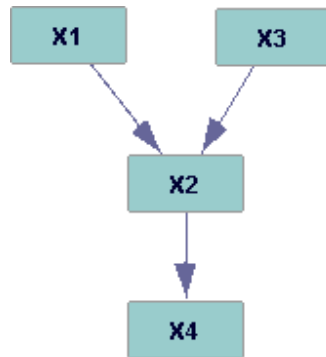
# Resimulation 3: Learn $G_2$ from $D_2$ , compare to $G_1$



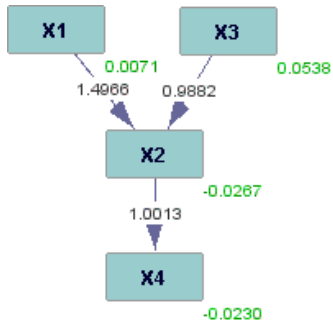
$G_2$  (right) contains 2 of the 3 edges in  $G_1$  (left), and no additional edges.

# Hsim 0: Data $D_1$ and Learned Graph $G_1$

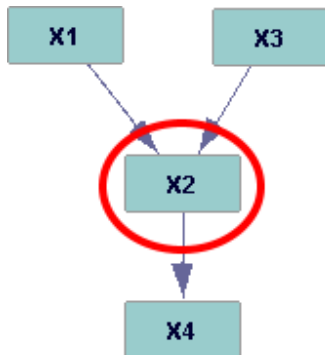
X1	X2	X3	X4
0.3596	-1.2491	-2.9277	-3.5328
1.2639	4.0011	1.2282	4.1915
0.8749	-1.7419	-1.6859	-2.2926
-2.1222	-0.3536	2.465	-0.2342
-0.9151	-2.7165	-2.3928	-4.5982
-0.5706	-3.802	0.0331	-4.7854
1.2468	0.5542	-0.7107	1.0888
1.1232	5.1059	0.7407	6.571
-1.4056	1.5811	-0.527	0.5514
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0.0751	-2.5419	-1.708	-1.8866
0.8523	2.0218	0.6163	2.7466
0.2440	0.7100	0.6777	0.0002



# Hsim 1: Fit $G_1$ to $D_1$ , making model $M_1$



## Hsim 2: Pick variables to resimulate



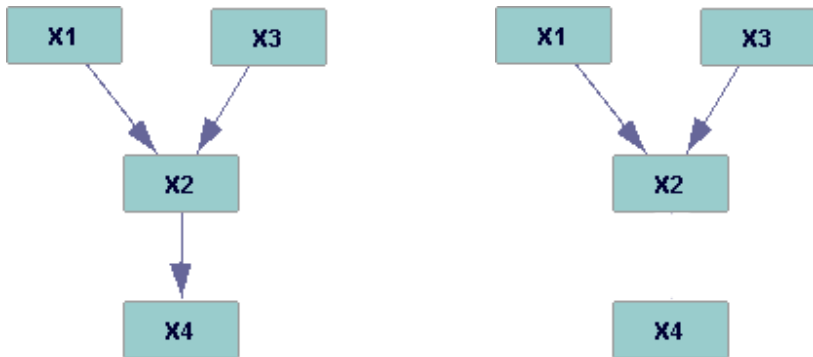
Variables can be selected or chosen at random.

## Hsim 3: Sample $D2$ from $M1$

X1	X2	X3	X4
0.3596	-0.3461	-2.9277	-3.5328
1.2639	-4.2367	1.2282	4.1915
0.8749	-2.4683	-1.6859	-2.2926
-2.1222	3.1447	2.465	-0.2342
-0.9151	-1.2284	-2.3928	-4.5982
-0.5706	-2.2541	0.0331	-4.7854
1.2468	-5.6872	-0.7107	1.0888
1.1232	-0.2238	0.7407	6.571
-1.4056	-4.6249	-0.527	0.5514
-0.2384	5.6388	-0.133	0.8222
0.0751	-1.8405	-1.708	-1.8866
0.8523	5.0506	0.6163	2.7466
0.2440	1.0460	0.6777	0.0002

Each row sampled from  $P_{M1}(X2|X1 = x1, X3 = x3, X4 = x4)$

## Hsim 4: Learn $G_2$ from $D_2$ , compare to $G_1$



$G_2$  (right) contains all edges oriented towards  $X_2$  in  $G_1$  (left).  $G_2$  contains no additional edges connected to  $X_2$ .

# Simulation Parameters

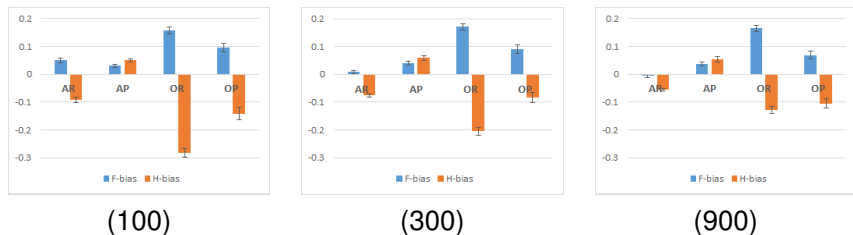
- Simulated 500 “true” graphs and sampled data.
- Run FGES and calculate actual accuracy measures.
- Estimate accuracy with full and hybrid resimulation.

Model parameters:

- Gaussian noise
- Functional relationships:
  - Linear
  - Nonlinear

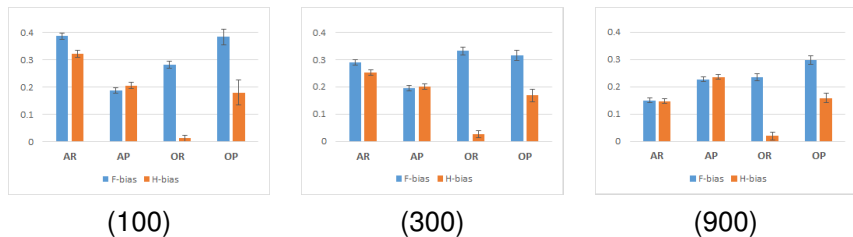


# Linear



**Figure:** Simulation study results for linear models, showing mean estimation errors for AR, AP, OR, and OP at sample sizes 100, 300, and 900. Error bars represent 95% confidence intervals of the mean estimates shown.

# Nonlinear



**Figure:** Simulation study results for nonlinear models, showing estimation errors for AR, AP, OR, and OP at sample sizes 100, 300, and 900. Error bars represent 95% confidence intervals of the mean estimates shown.

# Acknowledgements

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